## Bubble Sort

## Pseudocode implementation

The algorithm can be expressed as (0-based array):

```
procedure bubbleSort( A : list of sortable items )
    n = length(A)
    repeat
        swapped = false
        for i = 1 to n-1 inclusive do
            /* if this pair is out of order */
            if A[i-1] > A[i] then
                /* swap them and remember something changed */
                swap( A[i-1], A[i] )
                swapped = true
            end if
        end for
    until not swapped
end procedure
```


## Optimizing bubble sort

The bubble sort algorithm can be easily optimized by observing that the $n$-th pass finds the $n$-th largest element and puts it into its final place. So, the inner loop can avoid looking at the last $n-1$ items when running for the $n$-th time:

```
procedure bubbleSort( A : list of sortable items )
    n = length(A)
    repeat
        swapped = false
        for i = 1 to n-1 inclusive do
            if A[i-1] > A[i] then
                swap(A[i-1], A[i])
                swapped = true
            end if
        end for
        n = n - 1
    until not swapped
end procedure
```

More generally, it can happen that more than one element is placed in their final position on a single pass. In particular, after every pass, all elements after the last swap are sorted, and do not need to be checked again. This allows us to skip over a lot of the elements, resulting in about a worst case $50 \%$ improvement in comparison count (though no improvement in swap counts), and adds very little complexity because the new code subsumes the "swapped" variable:
To accomplish this in pseudocode we write the following:

```
procedure bubbleSort( A : list of sortable items )
    n = length(A)
    repeat
        newn = 0
        for i = 1 to n-1 inclusive do
            if A[i-1] > A[i] then
                swap(A[i-1], A[i])
                newn = i
            end if
            end for
            n = newn
    until n = 0
end procedure
```

Alternate modifications, such as the cocktail shaker sort attempt to improve on the bubble sort performance while keeping the same idea of repeatedly comparing and swapping adjacent items.

